

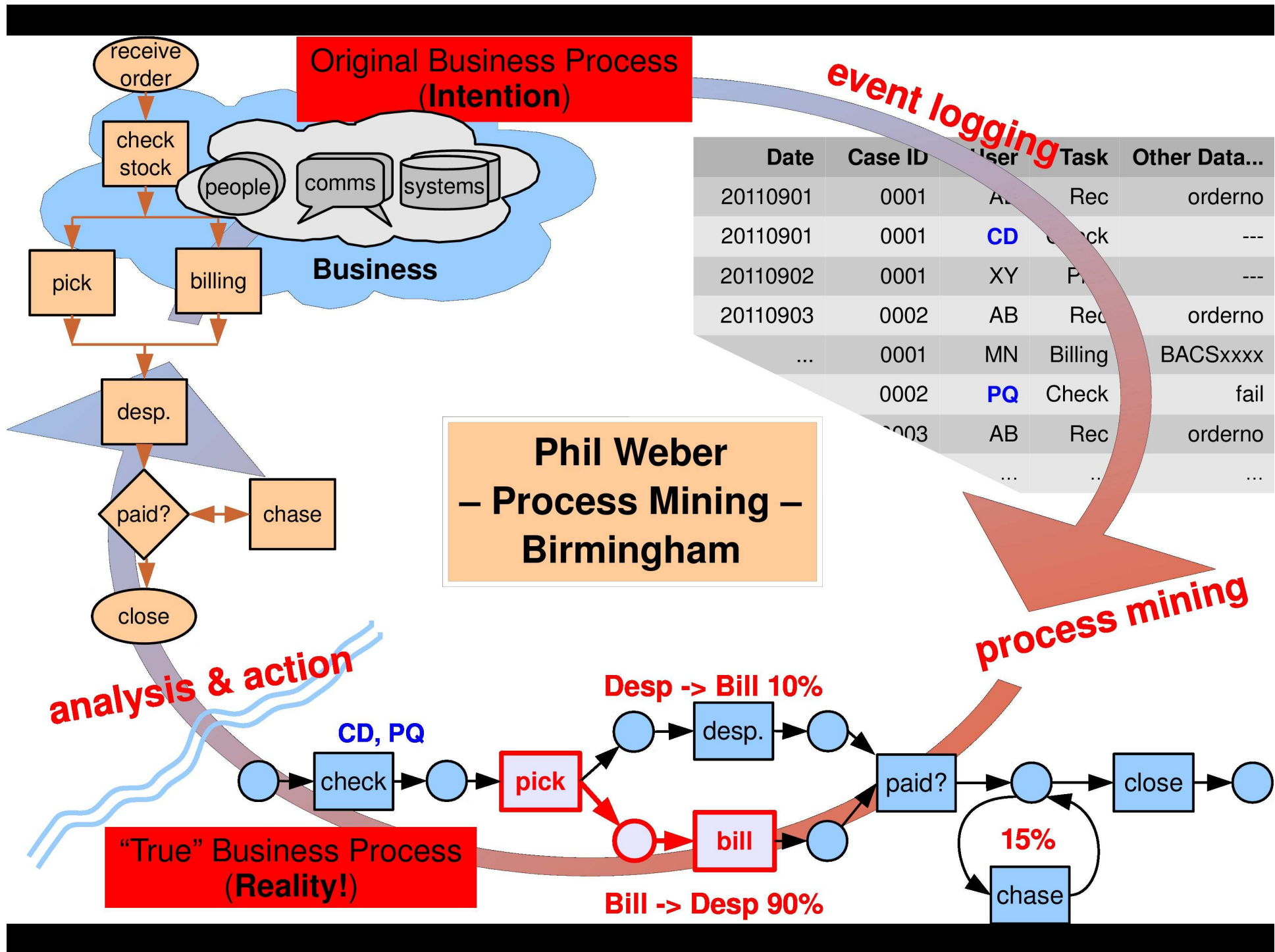


# Real-Time Detection of Process Change Using Process Mining

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# Changing Process

- Expected?
- Problem?

**How to detect?**



## Pre-requisites

1. Notion of Real-time
2. Measures of Models
3. Detect Change
4. Statistical Significance



## Notion of Real-time

### Predictability

### Results + timeframe

#### Accuracy vs Time

Accuracy:

$$Pr[d(P_M, P_{M_K}) > \epsilon] < \delta,$$

Mining Time:

$$t(\phi(L_k)) = A + k \cdot c < \eta.$$

Upper bound time  
Lower bound data

Requirement  
Realism

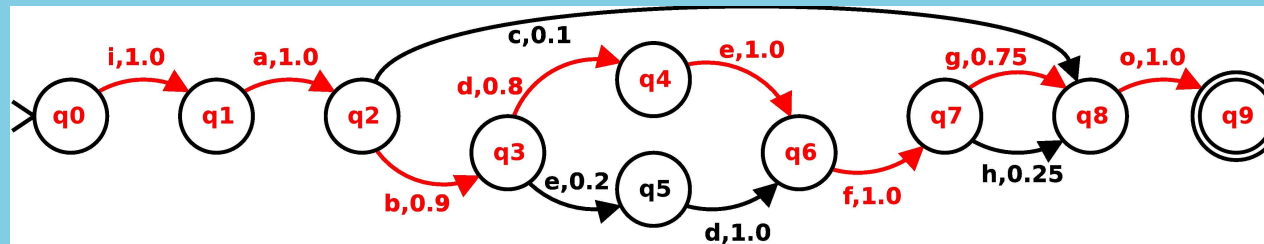


## Pre-requisites

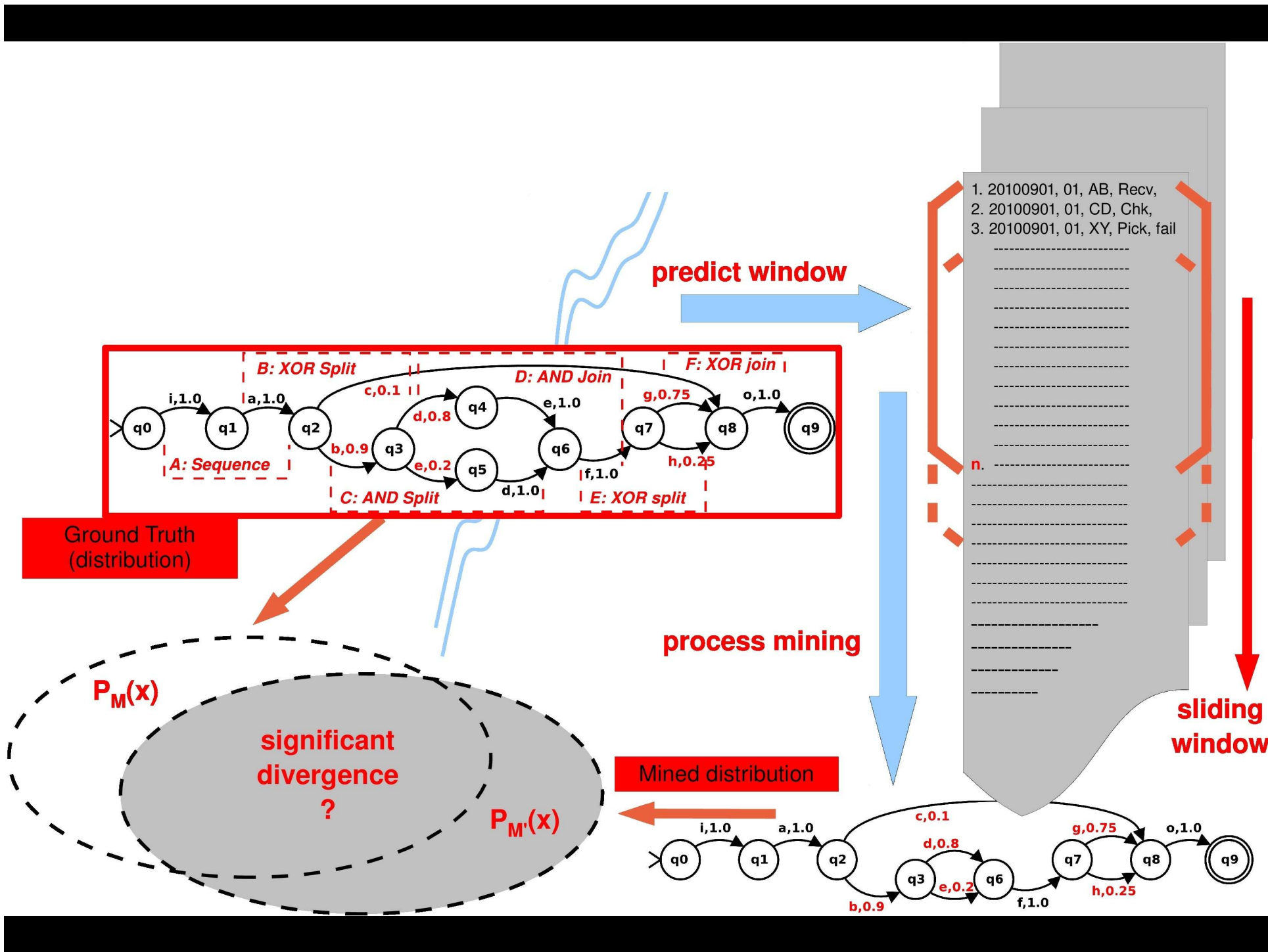
1. Notion of Real-time
2. **Measures of Models**
3. **Detect Change**
4. Statistical Significance

## Compare Models & Detect Change

### Probabilistic Representation



- Activities - symbols
- Traces - strings
- Distribution over strings
- PDFA





## Pre-requisites

1. Notion of Real-time
2. Measures of Models
3. Detect Change
4. **Statistical Significance**



## Statistical Significance

Sample from Distribution - Chi<sup>2</sup>

String/Arc Probability

- Hoeffding
- Hypothesis

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### Statistical Tests

Chi<sup>2</sup> Test:

$$\chi_s^2 = \sum_{i=1}^{i=k} \frac{(n(x_i) - n \cdot p(x_i))^2}{n \cdot p(x_i)}, \text{ and}$$

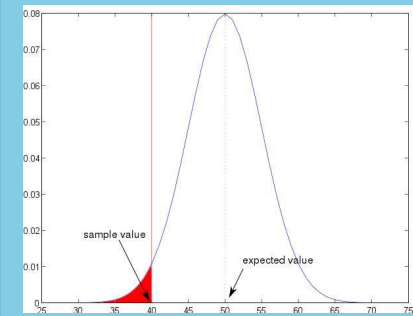
$$p = Pr(\chi_{k-1}^2 \geq \chi_s) = \int_{\chi_s}^{\infty} f(\chi_{k-1}^2) d(\chi_{k-1}^2).$$

Hoeffding Bound:

$$\forall a \in \Sigma, \left| \delta(q_1, a, q'_1) - \frac{f(q_2, a)}{n(q_2)} \right| < \sqrt{\frac{1}{2n(q_2)} \ln \left( \frac{2}{\alpha} \right)}.$$

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### Hypothesis Test





## Experimentation

Design & Predict

Simulate - Ground Truth

Mine "Sliding Window"

Compare Distributions

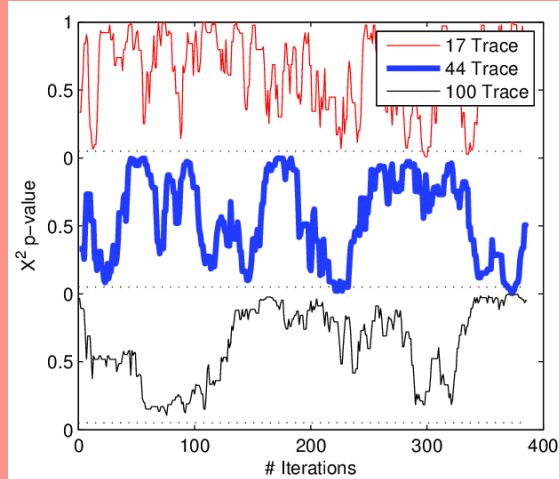
Statistical Tests

- vary probabilities *in* structures
- vary probabilities *of* structures
- vary how much data

## Results

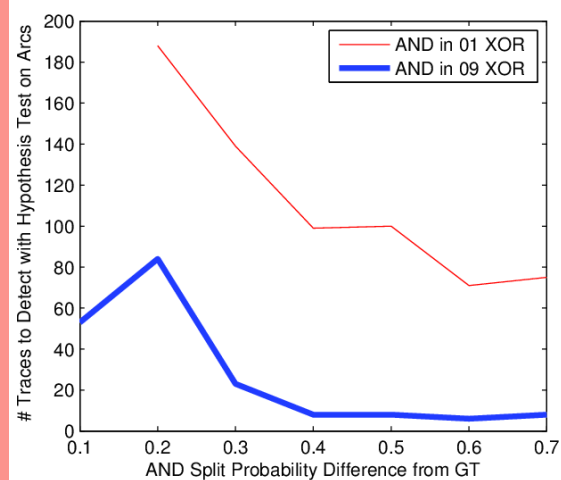
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### Chi<sup>2</sup> p-value - Unchanging Process



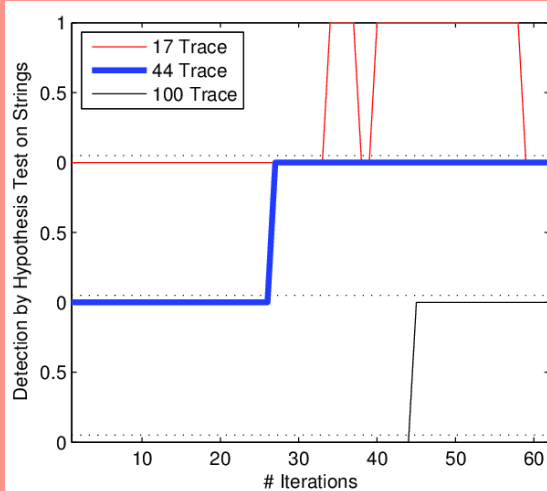
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### AND Split - Vary Probabilities



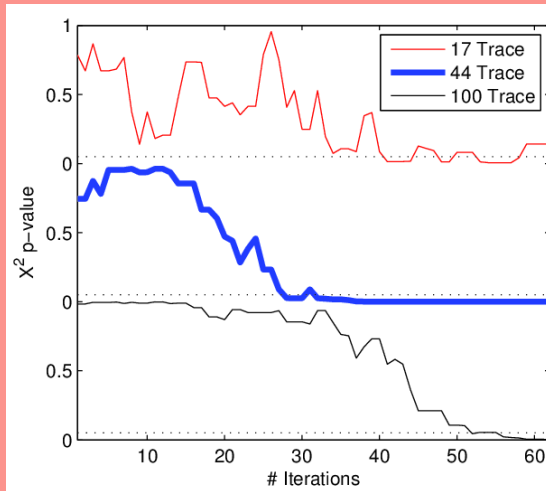
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### XOR Change - Hypothesis Testing



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### XOR Change - Chi<sup>2</sup>



# Questions & Thoughts?



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